

## *TECHNICAL COMMENT*

### A PROBLEM ON MARKOV CHAINS

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**Abstract.** A problem (arisen from applications to networks) is posed about the principal minors of the matrix of transition probabilities of a Markov chain.

**Keywords:** Markov chains, stochastic matrices.

#### 1. THE PROBLEM

Let the Markov chain  $(P^0, P)$  be given, where  $P$  is the  $n \times n$  matrix, whose entries are the transition probabilities, and  $P^0 \in [0, 1]^n$  is the initial distribution [1]. Every  $K \subseteq \{1, \dots, n\}$  identifies a principal minor of  $P$ , denoted by  $P_K$ ; let  $I_{|K|}$  be the identity matrix of order  $|K|$ . It is not difficult to show that

$$0 \leq \det(I_{|K|} - P_K) \leq 1, \quad \forall K \subseteq \{1, \dots, n\}$$

where  $\det$  denotes determinant. Is  $\det(I_{|K|} - P_K)$  a (conditioned or not) probability of an event related to Markov chain?

#### REFERENCE

- [1] S.N. Ethier and T.G. Kurtz, *Markov processes: Characterization and convergence*. J. Wiley, New York (1986).

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